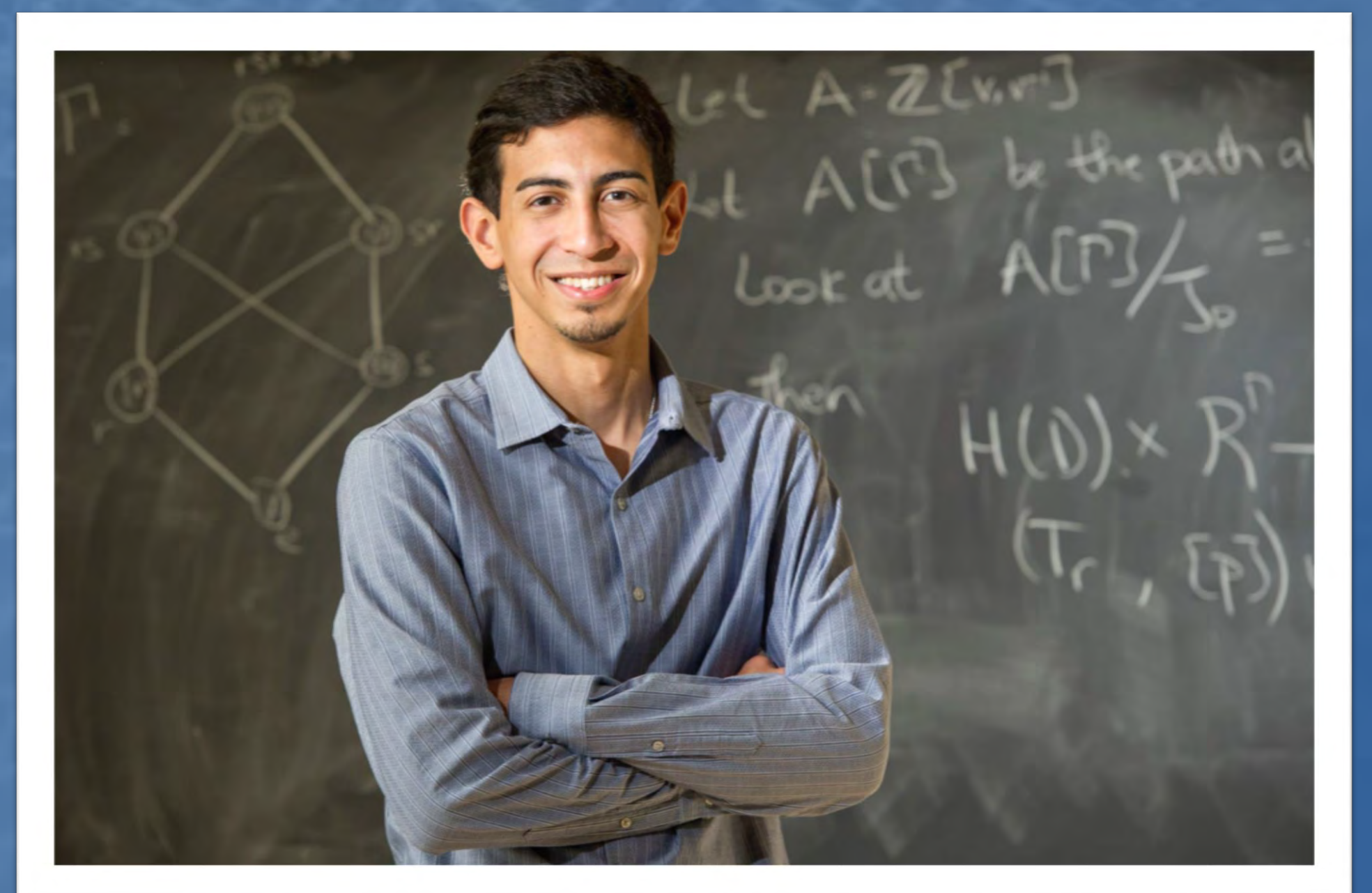


MATHEMATICS SEMINAR

PEAKS AND DESCENTS OF PERMUTATIONS

Given a permutation $\pi = \pi_1\pi_2 \cdots \pi_n \in \mathfrak{S}_n$, we say an index i is a peak if $\pi_{i-1} < \pi_i > \pi_{i+1}$. Let $P(\pi)$ denote the set of peaks of π . Given any set S of positive integers, define $P_S(n) = \{\pi \in \mathfrak{S}_n : P(\pi) = S\}$. In 2013, Billey, Burdzy, and Sagan showed that for all fixed subsets of positive integers S and sufficiently large n , $|P_S(n)| = p_S(n)2^{n-|S|-1}$ for some polynomial $p_S(x)$ depending on S . They conjectured that the coefficients of $p_S(x)$ expanded in a binomial coefficient basis centered at $\max(S)$ are all nonnegative. In this talk, we will share a recursive formula for $p_S(n)$ we use to prove that their “positivity conjecture” is true. It remains an open question to find a combinatorial meaning of these non-negative coefficients. Near the end of the talk, we will discuss various current developments regarding this topic, including some similar questions replacing “peaks” by “descents.” No prerequisites.

Friday, March 24th
3:30 pm – 4:30 pm
Seidler Hall 220



Alexander Diaz-Lopez, Ph.D.
Visiting Assistant Professor at Swarthmore College
2016-2018 Associate Editor for Notices of the AMS

REFRESHMENTS SPONSORED BY

