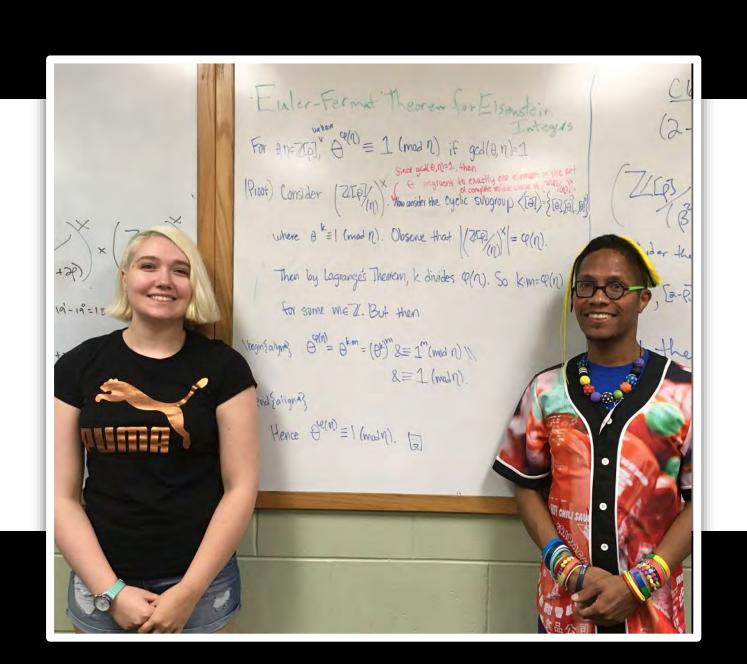
# MATHEMATICS SEMINAR

**FRIDAY** NOVEMBER 17<sup>TH</sup>, 2017 FLORIDA GULF COAST UNIVERSITY

**ROOM 100** MARIEB HALL 11:30 AM- 12:30 PM

### AN EULER PHI FUNCTION FOR THE EISENSTEIN INTEGERS AND SOME TANTALIZING APPLICATIONS



#### GUEST SPEAKERS:

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### **ABSTRACT:**

The Euler phi function on a given integer n yields the number of positive integers less than and relatively prime to n. Equivalently, it gives the order of the group of units in the quotient ring  $\mathbb{Z}/(n)$  for a given integer n. We generalize the Euler phi function to the Eisenstein integer ring  $\mathbb{Z}[\rho]$  where  $\rho$  is the primitive third root of unity  $e^{2\pi i/3}$  by finding the order of the group of units in the ring  $\mathbb{Z}[\rho]/(\theta)$  for any given Eisenstein integer  $\theta$ . As one application, we prove that the celebrated Euler-Fermat theorem holds for the Eisenstein integers. We also discuss the structure of certain unit groups  $(\mathbb{Z}[\rho]/(\gamma^n))^{\times}$  where  $\gamma$  is prime in  $\mathbb{Z}[\rho]$  and  $n \in \mathbb{N}$ , thereby generalizing wellknown results of similar applications in the integers and some lesser known results in the Gaussian integers.

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